

We determine the precise image of Atkin's  $U_p$  operator acting on reduced modular forms. The result holds for any level coprime to  $p$ . In particular, we determine the dimension of the kernel of  $U_p$  at weights  $k > p + 1$ . This contrasts with the low-weight case in which the dimension of the kernel is still very mysterious and erratic.